Differentiable Physics Simulations with Contacts: Do They Have Correct Gradients w.r.t. Position, Velocity and Control?

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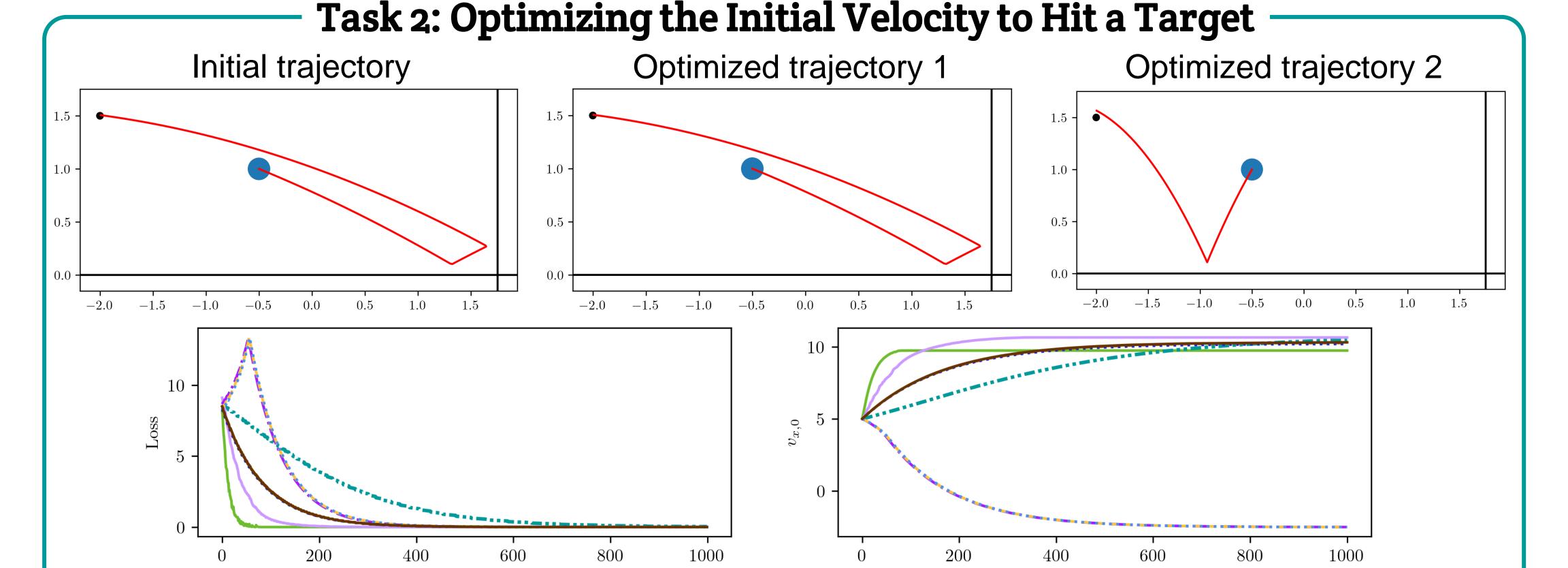


- Differentiable physics simulations make it easy to use gradient-based method for learning and control tasks and have huge potential in solving control and design problems.
- An increasing number of differentiable simulators are developed and open sourced.
- However, their performance has not been compared and benchmarked.

Differentiable Contact Models

| Contact Formulations | | impulses | Implementation choices |
|---|---------|----------|------------------------|
| Linear complementarity problems (LCPs) (w. TOI) | | | NimblePhysics |
| Convex Optimizations | w. TOI | velocity | DiffCoSim |
| | w/o TOI | | |
| Direct Velocity Impulse | w. TOI | | DiffTaichi |
| | w/o TOI | | |
| Position-based dynamics (PBD) | | position | Warp/Brax |
| Compliant models | | force | Warp/Brax |

TOI: time of impact, proposed by DiffTaichi to improve gradient calculation.



Task 3: Learning Optimal Control

Convex (w/ TOI)

Convex (w/o TOI)

Some implementations fail to learn the optimal control sequence.

Optimization iteration

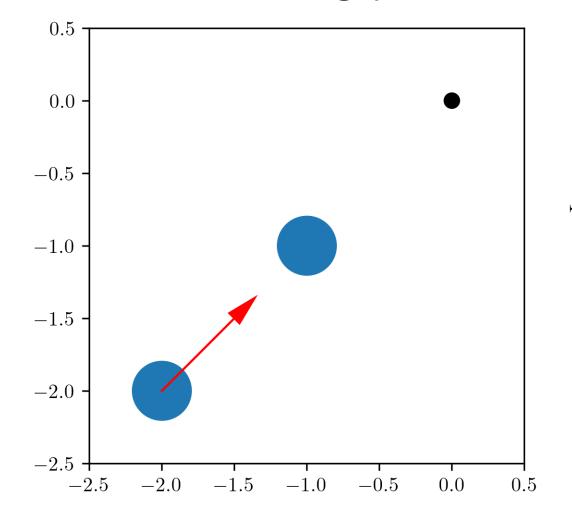
Compliant (Warp)

Compliant (Brax)

PBD (Warp)

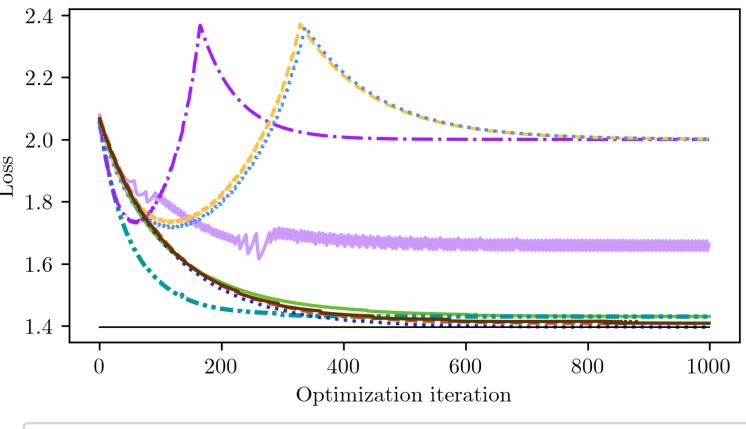
PBD (Brax)

Surprisingly, none of the calculated gradients match the analytical gradients.



PBD (Warp)

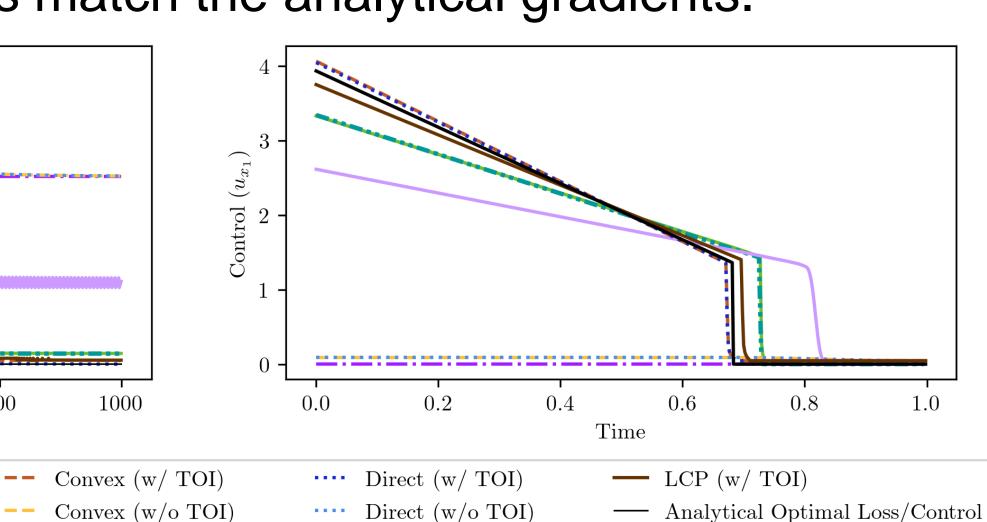
PBD (Brax)



Compliant (Warp)

- Compliant (Brax)

Convex (w/ TOI)



— LCP (w/ TOI)

Optimization iteration

Direct (w/TOI)

Direct (w/o TOI)